

Reg. No.

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B.E. / B.TECH. DEGREE EXAMINATIONS, MAY 2024
 Third Semester
MA22358 – TRANSFORM AND RANDOM PROCESSES
(Electronics and Communication Engineering)
(Regulation 2022)

TIME: 3 HOURS**MAX. MARKS: 100**

COURSE OUTCOMES	STATEMENT	RBT LEVEL
CO 1	Acquire the skill in examining a signal in another domain rather in the original domain by handling Full and Half Range Fourier Series.	3
CO 2	Develops the skill of conversion between time domain to frequency domain using the concept of Fourier Transforms and Z-transform.	3
CO 3	Express proficiency in handling higher order Partial differential equations.	3
CO 4	Reproduce and explain the basic concepts such as probability and random variable and identify the distribution. Acquire skills in handling situations involving more than one random variable.	3
CO 5	Apply the relationship within and between random processes.	3

PART- A (20 x 2 = 40 Marks)
 (Answer all Questions)

	CO	RBT LEVEL
1. Find the value of the Fourier series for $f(x) = \begin{cases} 0 & \in (-3,0) \\ 4 & \in (0,3) \end{cases}$ at the point of discontinuity $x = 0$.	1	2
2. Does $f(x) = \tan x$ possess a Fourier expansion?	1	2
3. If the Fourier series corresponding to $f(x) = x$ in the interval $(0, 2\pi)$ is $\frac{a_0}{2} + \sum_1^{\infty} \{a_n \cos nx + b_n \sin nx\}$, without finding the values of a_0, a_n, b_n find the value of $\frac{a_0^2}{2} + \sum_1^{\infty} (a_n^2 + b_n^2)$.	1	2
4. Find the R.M.S value of $y = x^4$ in $(-1, 1)$.	1	2
5. Find the Fourier transform of $f(x) = \begin{cases} 1, & 2 < x < 4 \\ 0, & \text{otherwise} \end{cases}$.	2	3
6. Find the Fourier cosine transform of $e^{-ax}, a > 0$.	2	3
7. Find Z-Transform of $\frac{1}{n}$.	2	2

8. Find $F(z)$ for the equation $f(n+2) - 3f(n+1) + 2f(n)=0$, if $f(0)=0$. 2 2
9. Find the PDE of the family of spheres having their centers on the Z-axis. 3 2
10. Eliminate the arbitrary function f from $z=f(y/x)$. 3 2
11. Form the PDE by eliminating arbitrary constant $z=ax^n+by^n$. 3 2
12. Solve $(D^3-3DD'^2+2D'^3)z=0$. 3 2
13. Test whether $f(x)=\begin{cases} |x|, & -1 \leq x \leq 1 \\ 0, & \text{otherwise} \end{cases}$ can be the probability density function of a continuous random variable? . 4 2
14. A random variable X can only take values 2 and 5. Given that the value 5 is twice as likely the value 2, determine the expectation of X . 4 2
15. The following table gives the joint probability distribution of X and Y , find the marginal distribution function of X and Y . 4 2

X			
	1	2	3
Y			
1	0.1	0.1	0.2
2	0.2	0.3	0.1

16. The regression equations are $3x + 2y = 26$ and $6x + y = 31$. Find the means of X and Y . 4 2
17. Consider a random process $X(t)=\cos(t+\phi)$, where ϕ is a uniform random variable in $\left(\frac{-\pi}{2}, \frac{\pi}{2}\right)$. Check whether the process is stationary. 5 2
18. If patients arrive at a clinic according to Poisson process with mean rate of 2 per minute. Find the probability that during a 1 minute interval, no patient arrives. 5 3
19. Find the variance of the stationary process $\{X(t)\}$ whose autocorrelation function is given by $R_{xx}(\tau)=25+\frac{4}{1+6\tau^2}$. 5 2

20. Determine the function $\frac{\omega^2}{\omega^6+3\omega^2+3}$ can or can't be a valid power density spectrum. 5 2

PART- B (5 x 10 = 50 Marks)

- | | Marks | CO | RBT LEVEL |
|---|-------|----|-----------|
| 21. (a) Expand $f(x) = \begin{cases} \pi+x, & -\pi \leq x \leq 0 \\ \pi-x, & 0 \leq x \leq \pi \end{cases}$ as a Fourier series and hence deduce that | (10) | 1 | 3 |

$$\sum_1^{\infty} \frac{1}{i^2} i$$

(OR)

- | | | | |
|--|------|---|---|
| (b) The table value of the function $y=f(x)$ is given below. Find a Fourier series up to the second harmonic to represent $f(x)$ in terms of x . | (10) | 1 | 3 |
|--|------|---|---|

X	0	π/3	2π/3	π	4π/3	5π/3	2π
Y	1.0	1.4	1.9	1.7	1.5	1.2	1.0

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|--|------|---|---|
| 22. (a) Find the Fourier sine transform and Fourier cosine transform of $f(x)=x^{n-1}$ and show that $\frac{1}{\sqrt{x}}$ is self reciprocal under both. | (10) | 2 | 3 |
|--|------|---|---|

(OR)

- | | | | |
|--|------|---|---|
| (b) Find $Z^{-1} \left[\frac{8z^2}{(2z-1)(4z+1)} \right]$ by convolution theorem. | (10) | 2 | 3 |
|--|------|---|---|

- | | | | |
|--|------|---|---|
| 23. (a) Solve: $(mz-ny)p+(nx-lz)q=ly-mx$. | (10) | 3 | 3 |
|--|------|---|---|

(OR)

- | | | | |
|---|------|---|---|
| (b) Solve: $(D^3-7D^2-6D)z=\sin(x+2y)+e^{2x+y}$ | (10) | 3 | 3 |
|---|------|---|---|

- | | | | |
|---|------|---|---|
| 24. (a) The probability mass function of random variable X is defined as $P(X=0)=3C^2$, $P(X=1)=4C-10C^2$, $P(X=2)=5C-1$, where $C>0$, and $P(X=r)=0$ if $r \neq 0,1,2$. Find (i) The value of C . | (10) | 4 | 3 |
|---|------|---|---|

(ii) $P((0 < X < 2) \vee (X > 0))$. (iii) The distribution function of X .

(iv) The largest value of x for which $F(x) < \frac{1}{2}$.

(OR)

(b) Two random variables have the joint PDF (10) 4 3

$$f(x, y) = \frac{x+y}{3}, 0 \leq x \leq 1, 0 \leq y \leq 2. \text{ Find the correlation coefficient.}$$

25. (a) Show that the random process $X(t) = A \cos \omega t + \theta$ is WSS if $A \wedge \omega$ are constants (10) 5 3
and θ is uniformly distributed random variable in $(0, 2\pi)$.

(OR)

(b) The autocorrelation function of random binary transmission $\{X(t)\}$ is given (10) 5 3

$$\text{by } R(\tau) = \begin{cases} 1 - \frac{|\tau|}{T}, & |\tau| \leq T \\ 0, & \text{elsewhere} \end{cases}, \text{ where } T \text{ is a constant. Find the power spectrum of}$$

the process $\{X(t)\}$.

PART- C (1 x 10 = 10 Marks)

(Q.No.26 is compulsory)

26. A random variable X has the following probability distribution

X	:	-2	-1	0	1	2	3
$P(X)$:	0.1	K	0.2	$2K$	0.3	$3K$

(i) Find K .

(ii) Evaluate $P(X < 2)$ and $P(-2 < X < 2)$.

(iii) Find the CDF of X .

(iv) Evaluate the mean of X .

Marks	CO	RBT LEVEL
(10)	4	3