

Reg. No.

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**B.E./ B.TECH. DEGREE EXAMINATIONS, MAY 2023**

Fourth-Semester

**CS18405 – DESIGN AND ANALYSIS OF ALGORITHMS***(Computer Science and Engineering)***(Regulation2018/2018A)****TIME:3 HOURS****MAX. MARKS: 100**

COURSE OUTCOMES	STATEMENT	RBT LEVEL
CO 1	The students will be able to analyze the running time of algorithms using asymptotic analysis	2
CO 2	The students will be able to describe the divide-and-conquer techniques and analyze the running time of the algorithms synthesizing those paradigms	2
CO 3	The students will be able to describe the dynamic programming and greedy paradigms and analyze the running time of the algorithms using those techniques	3
CO 4	The students will be able to employ linear programming and computational geometry methods to solve engineering problems	4
CO 5	The students will be able to describe the non-deterministic polynomial algorithms	5

**PART- A(10x2=20Marks)**

(Answer all Questions)

	CO	RBT LEVEL
1. Arrange the following functions in increasing orders of their growth. $n!$ , $\log n$ , $3^n$ , $n$ , $n^2$ , $n^3$ , $2^n$ , $n \log n$ .	1	2
2. State the three steps to be proved using a loop invariant.	1	2
3. Illustrate the significance of employing the 'divide and conquer' technique in algorithm design.	2	2
4. Derive the worst case time complexity of Merge sort using Master's theorem.	2	4
5. Compare dynamic programming and divide and conquer design technique.	3	3
6. Write the merits and demerits of greedy algorithms	3	3
7. Differentiate feasible and optimal solutions in linear programming	4	3
8. How simplex method identify optimal solution and determine whether the problem is infeasible or unbounded?	4	3
9. Derive the relationship of NP- complete problems with other classes P and NP- hard	5	4
10. Illustrate the backround of Clique problem.	5	4

PART- B (5x 14=70Marks)

Marks	CO	RBT LEVEL
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11. (a) Discuss insertion sort algorithm. Analyse its best and worst case complexity.

(14)	1	2
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(OR)

(b) (i) Discuss about the Big oh, big omega and big theta notations with suitable examples.

(7)	1	2
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(ii) Write a recursive algorithm to compute  $x^y$  and analyse it's complexity.

(7)	1	2
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12. (a) (i) Solve the recurrence relation using recursive tree method  $T(n)=4T(n/2) + n$ ;  $T(1)=1$

(7)	2	2
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(ii) Solve using masters method

(7)	2	2
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$$T(n) = 4T(n/2) + n^2$$

$$T(n) = 2 T(n/2) + n^3$$

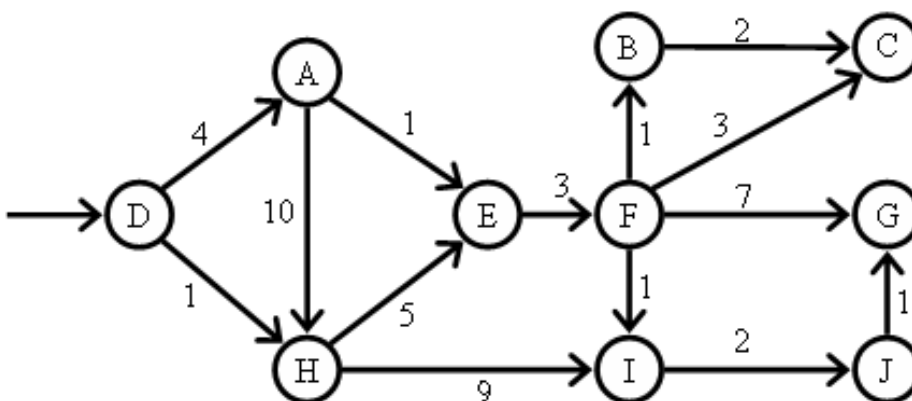
(OR)

(b) Discuss with an example, the working of finding closest pair of points in a Cartesian plane using divide-and-conquer strategy. Derive the complexity of the algorithm.

(14)	2	2
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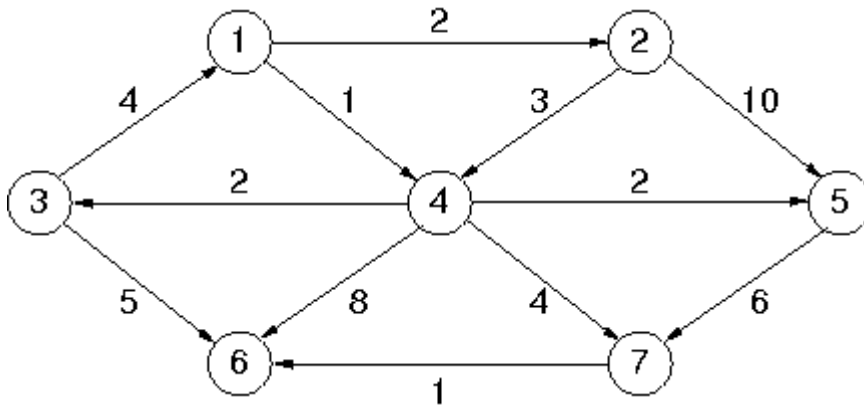
13. (a) Write the Dijkstra's algorithm. Find the shortest path from node 'A' to all other nodes using Dijkstra's algorithm.

(7)	3	3
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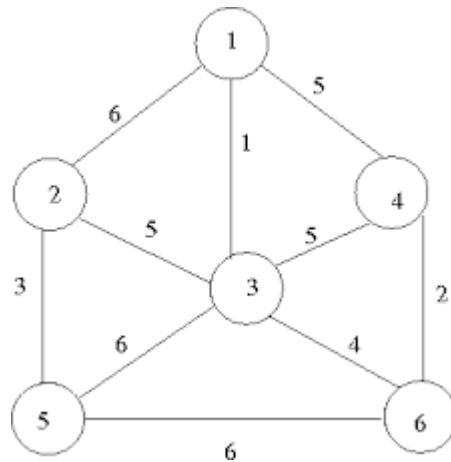


(OR)

- (b) (i) Find the MST for the following weighted graph using Prim's Algorithm. (7) 3 3



- (ii) Find the MST for the following weighted graph using Kruskal's Algorithm. (7) 3 3



14. (a) Solve the problem using Simplex method. (14) 4 3

Maximize  $Z = 5x_1 + 8x_2$

subject to constraints

$2x_1 + x_2 \leq 100$

$x_1 + 3x_2 \leq 90$

$x_1, x_2 \geq 0$

(OR)

- (b) Illustrate Graham's scan and Jarvis's march algorithms for the construction of convex hull with its complexity. (14) 4 3

**15. (a)** Analyse the background of Circuit satisfiability problem with example. **(14)** **5** **4**  
Prove that circuit satisfiability is NP-complete.

**(OR)**

**(b)** Analyse the background of the Vertex cover problem with example. Prove **(14)** **5** **4**  
that Vertex Cover is NP-complete.

**PART- C (1x 10=10Marks)**

(Q.No.16 is compulsory)

	<b>Marks</b>	<b>CO</b>	<b>RBT LEVEL</b>
<b>16.</b> Consider the list of marks obtained by 'n' students in a subject. Write an efficient algorithm to find and count the number of unique marks and display duplicate marks with its frequency. Analyse the algorithm's efficiency.	<b>(10)</b>	<b>1</b>	<b>5</b>